#### Light Flash Studies

At the impact of a high-velocity projectile on a thick target a small fraction of the kinetic energy is converted to radiant energy. The light intensity as a function of time as well as the optical spectrum can be observed. Friichtenicht<sup>8</sup> used iron microparticles and observed the light flash by twocolor photometry. He found that the blue part of the spectrum is increasing more rapidly with velocity than the red part. He observed a narrow (typically 0.2 µsec wide) fast risetime pulse of light followed by a much wider pulse (typically 10 µsec) which decays slowly to zero intensity. These observations are quite similar to results of Rollins and Jean<sup>9</sup> with bigger projectiles. They were able to measure more details because of the higher light intensity available. The projectiles were aluminum of cm size and were accelerated by a light gas gun. The target material was cadmium.

The first spike is continuum radiation and only present at the impact point. It is apparently due to a fast jet of material caused by the very high initial pressures. The peak intensity and the initial rate of change of intensity of the spike are proportional to  $v^8d^{\alpha}$  and  $v^6d^{2.1}$ , respectively, with v = projectile velocity, d = projectile diameter,  $\alpha = 0$ 2.9...4.0 (exact value depending on the wavelength used), and were found to be suitable to determine both diameter and velocity of a projectile if its composition is known.

The tail of the light flash is associated with a luminous ring expanding along the target plane. This ring is radiating in spectral lines which are characteristic of both target and projectile material. By analyzing the emission spectrum it is, in prinicpal, possible to determine the composition of the projectile.

#### Conclusion

As we have seen, there are three independent methods to determine velocity, mass, and composition of micrometeoroids. The light flash, however, is probably too faint and the emission spectrum too complicated as to lead to a practicable analysis. In order to investigate the crater, a very narrow beam of medium energy electrons and additional complicated instruments for electron and X-ray detection are necessary: volatile elements certainly escape observation. Analysis of the plasma seems to be the only practicable technique for micrometeoroid analysis onboard a spacecraft, although much additional effort is necessary to arrive at a quantitative method.

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# **Determination of the Energy Balance** of a Pulsed Plasma Source

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#### Introduction

ESIGN of a continuously working inductive plasma accelerator requires knowledge of the efficiency of energy exchange into the plasma. For basic information, it is sufficient to study the process of ionization, acceleration and heating of a pulsed accelerator. It is possible to obtain an approximate determination of the energy balance on the complete system by spectroscopically determining particle temperature, plasma velocity, and the damping rate of the oscillatory circuit of the system.

#### Measuring Instrumentation

The pulsed inductive acceleration device has been described in detail in Refs. 1 and 2. Helium gas, passing through a quick acting electromagnetic valve, enters the acceleration tube (pyrex glass) which is evacuated to a pressure lower than 10<sup>-5</sup> torr. The gas is ionized and accelerated by a singleturned conical coil across which a capacitor battery (6.5 µF. 10-15 kv) is discharged a defined time  $\Delta t$  (here 450  $\mu$ s) after opening the valve.

Spectroscopic measurements are carried out with optical interference filters. Signals are led through fiber optics to photomultipliers where they are registered on an oscilloscope screen. The optical arrangement was attached on a support which could be shifted along the acceleration tube. Thus, the arrival of the plasmoids at different positions could be observed and velocities determined. Simultaneously, the damping of the oscillating current with and without plasma generation and acceleration was measured using a pick-up coil.

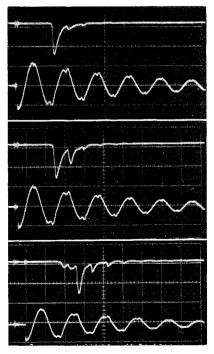


Fig. 1 Oscillograms of corresponding light intensities and pick-up voltages.

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#### Results

In Fig. 1, typical oscillograms for three charging voltages  $(U=15,\ 13.5,\ {\rm and}\ 10\ {\rm kv};$  from top to bottom) are presented. The upper signals show the corresponding light intensity of the He II (4686 Å) line emitted by the plasma. The lower signals are the pick-up coil voltages. The breakdown and simultaneous light emission for  $U=15\ {\rm kv}$  take place after one oscillation period. With decreasing U, a second peak appears after 1.5 periods (second plasmoid) which finally overcomes the first peak, because the first peak continuously vanishes (for  $U=10\ {\rm kv}$ ).

The total power input  $E_{\text{tot}}$  distributes in

$$E_{\text{tot}} = CU^2/2 = E_0 + E_{\text{pl}} \tag{1}$$

where  $E_0$  = losses in the circuit,  $E_{\rm pl}$  = energy absorbed by the plasma, and  $E_{\rm pl}$  distributes itself in

$$E_{\rm pl} \simeq E_{\rm ion} + E_{\rm therm} + E_{\rm kin}$$
 (2)

where  $E_{\rm ion}=$  ionization energy,  $E_{\rm therm}=$  energy for plasma heating, and  $E_{\rm kin}=$  kinetic energy of the accelerated plasma.

The value of  $E_{\rm pl}$  can be determined in first approximation from the damping of the discharge current which is described in Ref. 3. A resistance  $R_1 = R_0 + R_{\rm pl}$  is introduced ( $R_0 =$  loss resistance,  $R_{\rm pl}$  is an equivalent plasma resistance) which causes the same current as in the actual circuit. Thus, without plasma

$$E_{\text{tot}} = \int_{0}^{\infty} R_0 I_0^2(t) dt$$
 (3a)

with plasma

$$E_{\text{tot}} = \int_0^\infty R_1 I_1^2(t) dt \tag{3b}$$

Defining the efficiency of energy transfer

$$\eta = E_{\rm pl}/E_{\rm tot} \tag{4}$$

where  $I_0(t) = I_A f_0(t)$  and  $I_1(t) = I_A f_1(t)$  then

$$\eta = 1 - \int_0^\infty f_0^2(t)dt / \int_0^\infty f_1^2(t)dt$$
 (5)

The first amplitude  $I_A$  is equal for both currents (experimentally determined). With  $f_0(t) = \exp(-\alpha_0 t) \sin \omega t$  and  $f_1(t) = \exp(-\alpha_1 t) \sin \omega t$ , the efficiency simplifies under the condition  $\omega^2 \gg \alpha_0^2$  (this case:  $\omega = 7.7 \times 10^5 s^{-1}$ ,  $\alpha_0 = 2.8 \times 10^4 s^{-1}$ ) to

$$\eta = 1 - \alpha_0/\alpha_1 \tag{6}$$

In Fig. 2, values of  $\alpha_1$  are plotted as a function of U. Figure 3 shows values of  $E_{tot}$ ,  $\eta$ , and  $E_{p1}$  as functions of U. It must be realized, however, that the accelerated plasma remains only a short time  $t = t_2 - t_1$  in the influence of the coil

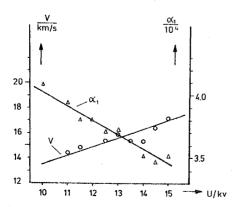


Fig. 2 Damping  $\alpha_1$  and measured plasma velocity vs capacitor voltage U.

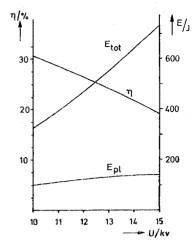


Fig. 3 Comparison of the total and absorbed energy as well as the efficiency.

and the effective efficiency is therefore

$$\eta_{\rm eff} = E_{\rm pl}/E_{\tau} = \eta \chi \tag{7}$$

where

$$E_{\tau} = \int_{t_1}^{t_2} R_1 I_1^2(t) dt$$

A corresponding calculation yielded  $\chi = 3$ .

The plasma velocity is determined by measuring the onset of the light intensity pulses at three different positions along the acceleration tube. Results are given in Fig. 2.

The electron temperature  $T_e$  was determined from the ratio of the two He lines of subsequent ionization stages  $I_{\rm II}/I_{\rm I}$ :

$$I_{\rm II}/I_{\rm I} = C(1/b_{\rm L}/N_c)(kT_c)^{3/2} \exp(-52.5/kT_c)$$
 (8)

where C contains atomic constants,  $b_{1.1}$  is the ratio of the population density of the He II ground state to the corresponding Saha-Boltzmann density (tabulated in Ref. 4). The density  $N_e$  for  $T_e = 50,000^{\circ}$ K was known from earlier measurements (see Ref. 5). A change of  $N_e$  with  $T_e$  could be estimated from the intensity of the He II (4686 Å) line. The ratio of the fourth level to the ground level of the He II ion,  $N_4/N_1$  is calculated over a wide  $N_e$  and  $T_e$  range for a nonthermal plasma. For these conditions  $N_1$  is set equal to  $N_e$  with  $\pm 30\%$ :

$$N_4/N_1 \approx N_4/N_e = f(N_e, T_e) \tag{9}$$

Since  $T_{\epsilon}(U)$  is known and  $I_{II}$  is proportional to  $N_4$ , then  $N_{\epsilon} = N_{\epsilon}(U)$ .

In Fig. 4, the temperature  $T_e$  is plotted as a function of U To calculate the thermal and kinetic energy of the plasma the total number of charged particles in the plasmoids must be known. The maximum density ( $\approx 1.2 \times 10^{16} \text{cm}^{-3}$  for peak 1;  $\approx 7.7 \times 10^{15} \text{cm}^{-3}$  for peak 2) and the density distribution over the plasma length is nearly constant from 10 to 15 kv. The plasmoids have an annular shape and their volume was estimated in Ref. 5. Thus a total particle

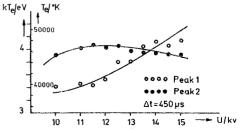


Fig. 4 Electron temperature of both plasmoids.

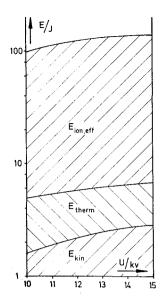


Fig. 5 Energy balance in function of capacitor voltage.

number of  $2 \times 10^{18}$  and  $1 \times 10^{18}$  for the 1st and 2nd plasmoid, respectively, is obtained.

In Fig. 5, the resulting energy balance is presented as a function of U. The effective ionization energy  $E_{\text{ion,eff}}$  was calculated using Eq. (2).

#### Discussion

This investigation did not serve so much as to study the acceleration of a plasma, but rather to get information on a continuously working plasma source with a well-defined initial plasma velocity v. It can be seen from Fig. 2 that v varies slowly with U. As known from earlier investigations, the oscillating frequency f has a strong influence on v. This will be investigated by further measurements. Fig. 3 shows that an increase of  $E_{\rm tot}$  up to a factor larger than two yields only an increase in  $E_{\rm pl}$  of about 40%, because  $\alpha_{\rm l}$  decreases with increasing U. The main portion of  $E_{\rm pl}$  (Fig. 5) is needed for the ionization energy  $E_{\rm ion.eff}$  (more than 90%), whereas  $E_{\rm kin}$  and  $E_{\rm therm}$  attain only small values.

As seen from the energy balance (Fig. 5),  $E_{\text{ion,eff}}$  per particle is about ten times the theoretical value which is  $4 \times 10^{-18} J/\text{particle}$ . Because of technical and physical reasons, the realizable range of particle flux N for continuously working accelerators is about  $10^{20}-10^{21}$  particles/sec. Thus, the necessary power requirement  $P_{\text{pl}}$  for such a source can be estimated approximately

$$P_{\rm pl} \approx \dot{N} \; {\rm (particles/s)} \cdot E_{\rm ion,eff} (J/{\rm particles})$$

Therefore,  $P_{\rm pl}$  is 5 kw  $\lesssim P_{\rm pl} \lesssim$  50 kw. The value of the effective efficiency of energy transfer  $\eta_{\rm eff}$  (Eq. 7) was about 60–90% for the pulsed accelerator, so that assuming similar values for the continuous accelerator the power requirement must be divided by the corresponding  $\eta_{\rm eff}$ .

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# Laminated Orthotropic Plates under Transverse Loading

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#### Introduction

THE use of high performance composites for lightly loaded structures leads to a small number of plies, thus producing asymmetrical laminates. These plates exhibit coupling between bending and stretching as was shown by Reissner and Stavsky¹ for two layer plates. Laminates which are symmetric about the reference surface do not produce coupling and behave as homogeneous anisotropic plates.

Stavsky<sup>2</sup> has established a linear theory for multilayer aeolotropic plates, based on the Kirchhoff hypothesis, and shown the reduction to a single eighth order equation for a generalized stress function. He gave solutions for cylindrical bending and uniform distribution of stress resultants and couples. Whitney and Leissa<sup>3</sup> have given a formulation for heterogeneous anisotropic plates and the reduction to three equations that are expressed in terms of displacements. They presented solutions for sinusoidal transverse loading, vibration, and buckling of cross-ply and angle-ply laminates. These plates have an even number of layers of the same thickness and elastic properties. The layers are alternately oriented at 0° and 90° to the plate axes for the cross-ply laminate and  $\pm \theta$  for the angle-ply. Whitney expanded each displacement in a double Fourier series and gave solutions for cross-ply and angle-ply plates under transverse load.

Whitney and Leissa<sup>5</sup> used a formulation in terms of a stress function and transverse displacement given by Dong, Pister and Taylor<sup>6</sup> and expanded both dependent variables in double Fourier series. They presented solutions for crossply and angle-ply plates under uniform transverse load, vibration and buckling. The Ritz technique was used by Ashton and Waddoups<sup>7</sup> to minimize the energy expression for symmetric anisotropic plates. Beam vibration modes were used for the assumed deflection functions and they studied displacement under lateral load, vibration and buckling

This study uses the generalized stress function equation<sup>2</sup> and develops a Navier type of solution for simply supported, arbitrarily laminated, orthotropic plates under transverse loadings. The plate may have any number of orthotropic layers of arbitrary thicknesses and elastic properties with axes of elastic symmetry coincident with the plate axes. Deflection, stress resultants and couples are given explicitly

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